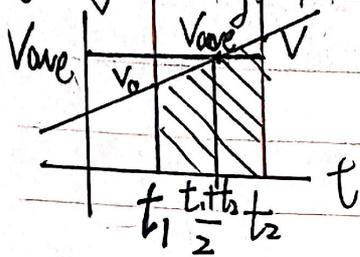


~ The "Big Five"



① $V_{ave} = \frac{v_0 + V}{2}$

② $\Delta X = v_0 \Delta t + \frac{1}{2} a (\Delta t)^2$

③ $\Delta X = V \Delta t - \frac{1}{2} a (\Delta t)^2$

④ $V = v_0 + a \Delta t$

⑤ $2a \Delta X = V^2 - v_0^2$

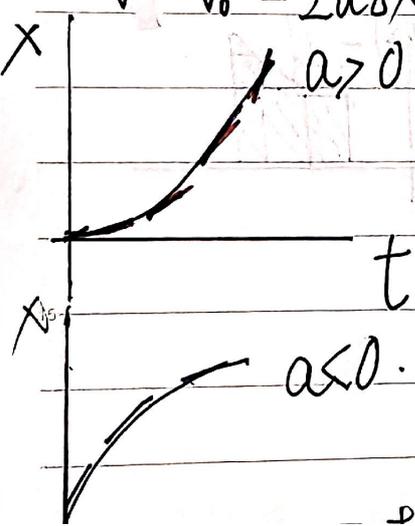
$\frac{m a \Delta X = m \frac{1}{2} V^2 - m \frac{1}{2} v_0^2}{F}$

$V_{ave} = \frac{V + v_0}{2}$ $t = \frac{\Delta V}{a} = \frac{V - v_0}{a}$

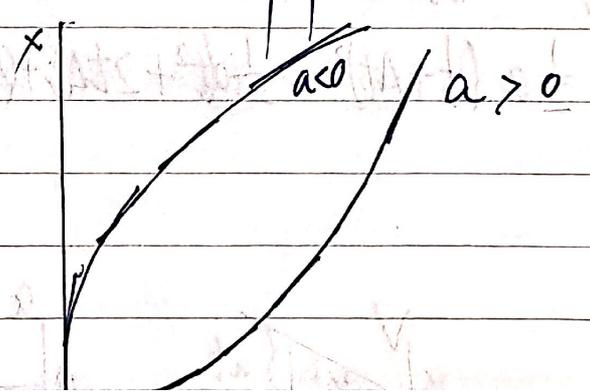
$V_{ave} t = \Delta X$

$\frac{V + v_0}{2} \cdot \frac{V - v_0}{a} = \Delta X$

$V^2 - v_0^2 = 2a \Delta X$



x-t 图中
斜率 $\Rightarrow v$
斜率 $\uparrow \Rightarrow a \uparrow$
 $a \Rightarrow$ 斜率变化量 Δv



5. Free fall

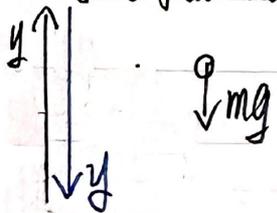
a. $g = 9.8 \text{ m/s}^2$
 $= \frac{W}{m}$

$\downarrow mg$

b. local gravity mg

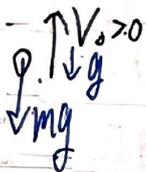
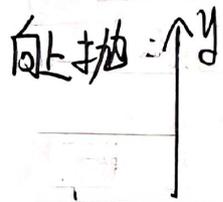
c. free fall with initial velocity

$a = \frac{F}{m} = -g$
 $= +g$



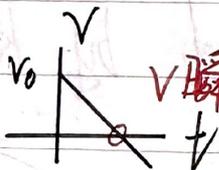
以向下为正: $v_0 = 0$ $v = gt$ $y = \frac{1}{2}gt^2$

向上 $v = -gt$ $y = -\frac{1}{2}gt^2$



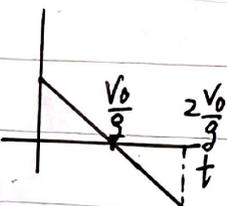
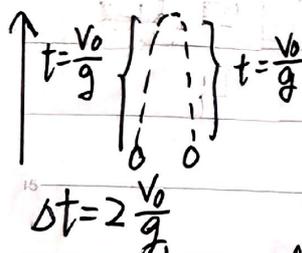
$a = -g$

$v = v_0 - gt$



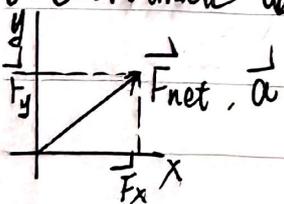
v 瞬间为 0 达到最高点 $t = \frac{v_0}{g}$

$y = y_0 + v_0 t - \frac{1}{2}gt^2$



$\Delta t = 2 \frac{v_0}{g}$

b. Coordinate decomposition



$\vec{F} = m\vec{a}$

$\vec{F}_x + \vec{F}_y = m\vec{a}_x + m\vec{a}_y$

$0 = \underbrace{F_x - ma_x}_x = \underbrace{ma_y - F_y}_y / (\underbrace{F_x - ma_x}_x) + (\underbrace{F_y - ma_y}_y) = 0$

$\begin{cases} F_x = ma_x \\ F_y = ma_y \end{cases}$

竖直上抛

$\begin{cases} v_t = gt \\ h = \frac{1}{2}gt^2 \\ v_t^2 = 2gh \end{cases}$

$\begin{cases} v_t = -gt \\ h = v_0 t - \frac{1}{2}gt^2 \\ v_t^2 - v_0^2 = -2gh \end{cases}$

3. Newton's 2nd law

a. Inertia

Inertial mass : m .

b. 2nd law

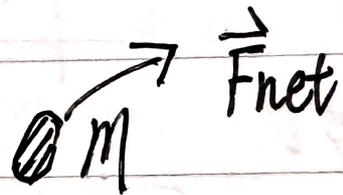
$$\vec{F}_{\text{net}} = 0 \iff \vec{a} = 0$$

$$\vec{F}_{\text{net}} \propto m\vec{a}$$

$$\vec{a} \propto \frac{\vec{F}_{\text{net}}}{m}$$

$$\vec{F} = m\vec{a}$$

$$\vec{a} = \frac{\vec{F}}{m}$$

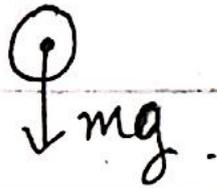


$$\vec{a}(\vec{F}_{\text{net}}, m)$$

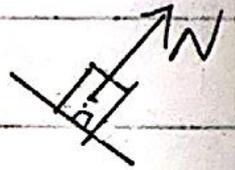
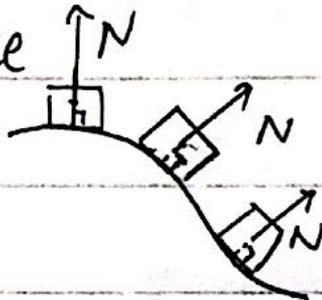
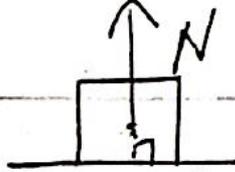
$$\vec{F}_{\text{net}} = m\vec{a}$$

Toy Model Forces

a. Gravity



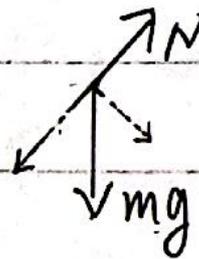
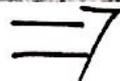
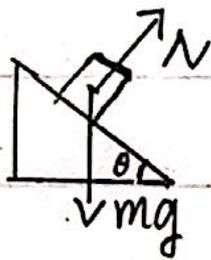
b. Normal Force



Prependicular. $\vec{N} \perp \text{surface}$.

e.g.

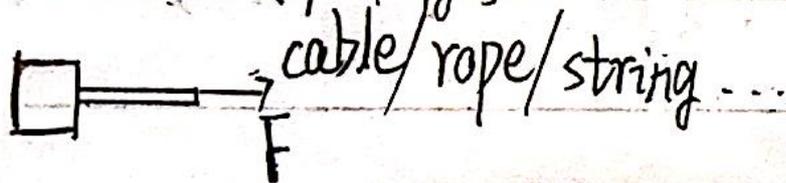
rest.



Only 2 Forces: N and mg

$$0 = ma_y = N - mg \cos \theta \Rightarrow N = mg \cos \theta$$

c. Tension (pulling force)



T T (tension in the rope).



d. Friction (passive) (tangential)

$$\vec{F}_{\text{net}} = m\vec{a}$$

i. Kinematic friction μN

$$f_k = \mu N \quad \mu: \text{coefficient of friction}$$

ii. Static friction 受力分析

$$f_s = F(\text{pull}) / (\text{push}) \dots \text{eg. } \begin{array}{c} \leftarrow f_s \\ \text{---} \\ \rightarrow F \end{array} \quad \begin{array}{l} a=0 \\ v=0 \end{array}$$

$$f_s \leq f_k \Rightarrow f_s \leq \mu N$$

when $f_s = f_k = \mu N$, $f_s \propto N$

e. Drag

$$f = \beta v$$

e.g.

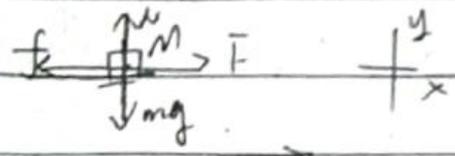


$$a = \frac{mg - \beta v}{m} \\ = g - \frac{\beta}{m} v$$

\Rightarrow when $a=0$, Terminal speed = $V_{\text{terminal}} = \frac{mg}{\beta}$
($g - \frac{\beta}{m} v = 0$)

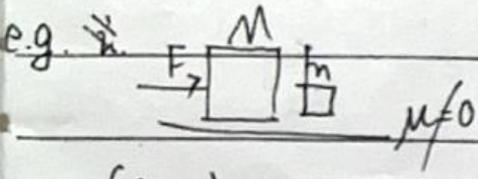
Mechanics

a. Horizontal Surface.



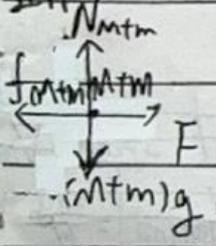
$$\begin{cases} ma = F - f \\ 0 = N - mg \\ f = \mu mg \end{cases} \rightarrow a$$

$$a = \frac{F_{\text{net}}}{m} = \frac{F - f}{m} = \frac{F - \mu mg}{m}$$

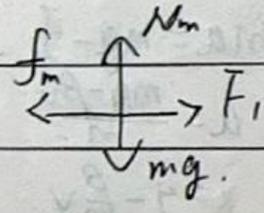
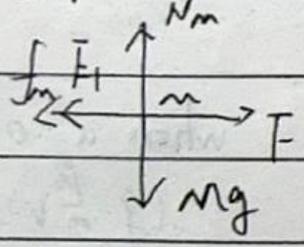


$(M+m)a = F$

整体: $a = \frac{F}{M+m}$



分析:



$$\begin{cases} Ma = F - f_m = F_1 - \mu mg \\ Ma = F - F_1 - f_m = F - F_1 - \mu Mg \end{cases} \Rightarrow (M+m)a = F - \mu(M+m)g$$

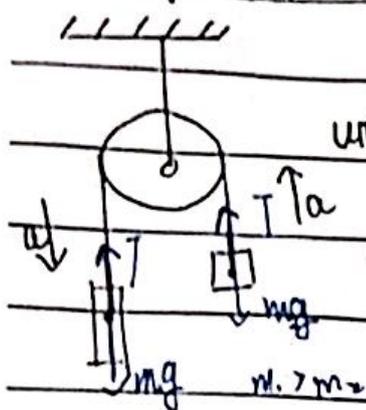
$$a = \frac{F}{M+m} - \mu g$$

$$F_1 = ma + \mu mg = m(a + \mu g) = \frac{m}{M+m} F$$

$\mu=0$: $F_{\text{net}_2} = F - F_1 = \frac{m}{M+m} F$

b. Atwood Machine

75 | \vec{i} internal forces



$$m_1 a = T - m_1 g$$

$$m_2 a = m_2 g - T$$

$$(m_1 + m_2) a = (m_1 - m_2) g$$

$$a = \frac{m_1 - m_2}{m_1 + m_2} g$$

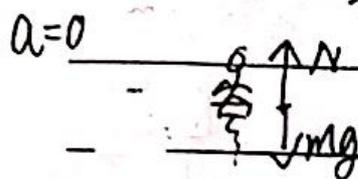
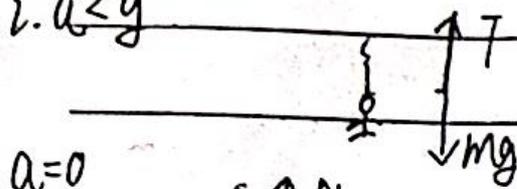
$$T = m_1 (g - a)$$

$$= m_1 \left(g - \frac{m_1 - m_2}{m_1 + m_2} g \right)$$

$$= m_1 g \left(\frac{2m_2}{m_1 + m_2} \right) = 2 \frac{m_1 m_2}{m_1 + m_2} g$$

c. Apparent Weight

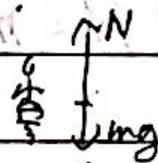
i. $a < g$



$$N = mg$$

$$T = mg$$

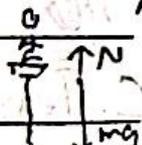
$a \uparrow$



$$N - mg = ma$$

$$T - mg = ma$$

$a \downarrow$

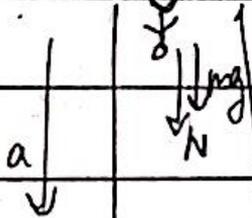


$$mg - N = ma$$

ii. $a = g$

$$\text{Nor } T = m(g - a) = 0$$

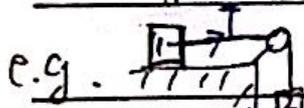
iii. $a > g$



$a = 2g$

$$N + mg = ma$$

d. Another Atwood Machine



$$\begin{cases} m_1 a = T - \mu m_1 g \\ m_2 a = m_2 g - T \end{cases}$$

$$\Rightarrow (m_1 + m_2) a = (m_2 - \mu m_1) g$$

$$a = \frac{m_2 - \mu m_1}{m_1 + m_2} g$$

$$T = m_2 (g - a)$$